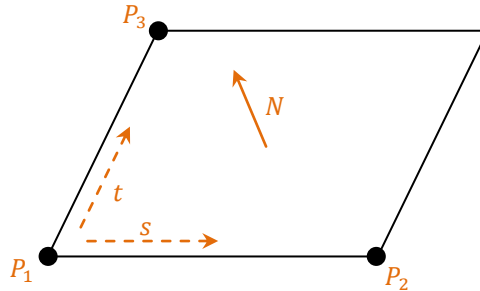


Parametric Plane

A plane can be described as a set of parametric equations from three points P_1 , P_2 , and P_3 and two parameters s and t .



$$\begin{aligned}x &= x_1 + (x_2 - x_1) \cdot s + (x_3 - x_1) \cdot t \\y &= y_1 + (y_2 - y_1) \cdot s + (y_3 - y_1) \cdot t \\z &= z_1 + (z_2 - z_1) \cdot s + (z_3 - z_1) \cdot t\end{aligned}$$

The normal vector N can be calculated by taking the cross product of the vectors between the points.

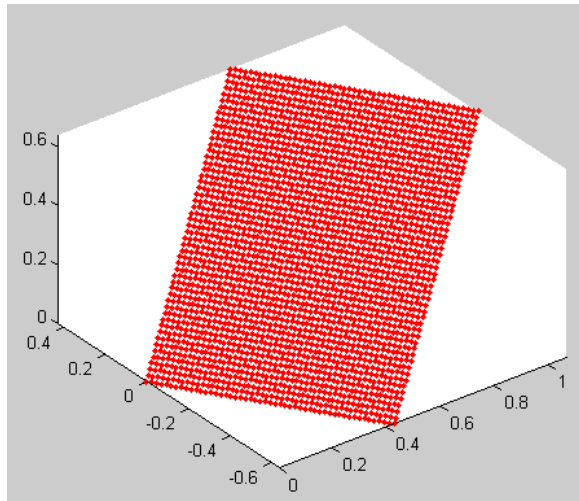
$$N = (P_2 - P_1) \times (P_3 - P_1)$$

When expanded out becomes:

$$\begin{aligned}N_x &= (y_2 - y_1) * (z_3 - z_1) - (z_2 - z_1) * (y_3 - y_1) \\N_y &= (z_2 - z_1) * (x_3 - x_1) - (x_2 - x_1) * (z_3 - z_1) \\N_z &= (x_2 - x_1) * (y_3 - y_1) - (y_2 - y_1) * (x_3 - x_1)\end{aligned}$$

The directions of s and t do not need to be orthogonal, however this is typically suggested for defining a plane. When s and t are parallel, the plane collapses to a line in the direction of s . If s and t are non-parallel, but not orthogonal, the plane will still be uniquely defined, but the point spacing in s and t becomes sheared and less intuitive.

An example parametric plane is shown below, with an orthogonal s and t . The points are sampled evenly in s and t .



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